## NLP Tasks and Linear Classification

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#### A Landscape of Al



## What do NLPers actually do?

 The best resource to be acquainted with NLP research is conference proceedings

#### **SUBMISSIONS**

ACL 2019 has the goal of a broad technical program. Relevant topics for the conference include, but are not limited to, the following areas (in alphabetical order):

- Applications
- Dialogue and Interactive Systems
- Discourse and Pragmatics
- Document Analysis
- Generation
- Information Extraction and Text Mining
- Linguistic Theories, Cognitive Modeling and Psycholinguistics
- Machine Learning
- Machine Translation
- Multidisciplinary
- Multilinguality
- Phonology, Morphology and Word Segmentation
- Question Answering
- Resources and Evaluation
- Sentence-level semantics
- Sentiment Analysis and Argument Mining
- Social Media
- Summarization
- Tagging, Chunking, Syntax and Parsing
- Textual Inference and Other Areas of Semantics
- Vision, Robotics, Multimodal, Grounding and Speech
- Word-level Semantics

Call for papers (ACL 2019)

#### But they're usually out-of-date



## What do NLPers actually do?

• The best resource to be acquainted with NLP research is conference proceedings Table of Contents of ACL'19





## A Few Applications of NLP

- Linguistic aspects
  - Part-of-speech tagging, parsing
- Natural language understanding
  - Sentiment classification, relation extraction
  - Question answering, machine comprehension
- Natural language generation
  - Machine translation, text summarization, dialogue systems

Researchers like to invent new tasks to publish more papers

Question: Suppose we have N models and M tasks, how many papers can we publish?  $2^{N+M} - N - M + 1$ 

## Why is NLP important?

- Related to the core of AI
  - One of the most difficult area that AI hasn't conquered
  - Many unsolved scientific problems
- Bringing revenues for companies



## Why is NLP difficult?

- Ambiguity
  - Word sense disambiguation

I went to the **bank** to deposit some money. I got wet on the river **bank**.



## Why is NLP difficult?

- Ambiguity
  - Word sense disambiguation

I went to the **bank** to deposit some money.

I got wet on the river **bank**.

- Coreference resolution

The book doesn't fit into the bag, because **it** is too small The book doesn't fit into the bag, because **it** is too big





## Why is NLP difficult?

- Subtlety
  - Word sense disambiguation
    - How many senses?
- The **bank** was on fire

#### The **bank** blocked my credit card

WordNet http://wordnetweb.princeton.edu/perl/webwn WordNet Search - 3.1

- WordNet home page - Glossary - Help

Word to search for: bank Search WordNet

Display Options: (Select option to change) ᅌ Change

Key: "S:" = Show Synset (semantic) relations, "W:" = Show Word (lexical) relations
Display options for sense: (gloss) "an example sentence"

#### Noun

- <u>S:</u> (n) **bank** (sloping land (especially the slope beside a body of water)) "they pulled the canoe up on the bank"; "he sat on the bank of the river and watched the currents"
- <u>S:</u> (n) <u>depository financial institution</u>, **bank**, <u>banking concern</u>, <u>banking</u> <u>company</u> (a financial institution that accepts deposits and channels the money into lending activities) *"he cashed a check at the bank"; "that bank nords the mortgage on my nome*
- <u>S:</u> (n) bank (a long ridge or pile) "a huge bank of earth"
- <u>S:</u> (n) **bank** (an arrangement of similar objects in a row or in tiers) *"he operated a bank of switches"*
- <u>S:</u> (n) **bank** (a supply or stock held in reserve for future use (especially in emergencies))
- <u>S:</u> (n) **bank** (the funds held by a gambling house or the dealer in some gambling games) *"he tried to break the bank at Monte Carlo"*
- <u>S:</u> (n) **bank**, <u>cant</u>, <u>camber</u> (a slope in the turn of a road or track; the outside is higher than the inside in order to reduce the effects of centrifugal force)
- <u>S:</u> (n) <u>savings bank</u>, <u>coin bank</u>, <u>money box</u>, **bank** (a container (usually with a slot in the top) for keeping money at home) *"the coin bank was empty"*
- <u>S:</u> (n) bank, <u>bank building</u> (a building in which the business of banking transacted) *"the bank is on the corner of Nassau and Witherspoon"*
- <u>S:</u> (n) **bank** (a flight maneuver; aircraft tips laterally about its longitudinal axis (especially in turning)) *"the plane went into a steep bank"*

#### Verb

- <u>S:</u> (v) bank (tip laterally) "the pilot had to bank the aircraft"
- <u>S:</u> (v) bank (enclose with a bank) "bank roads"
- <u>S:</u> (v) **bank** (do business with a bank or keep an account at a bank) "Where do you bank in this town?"
- <u>S:</u> (v) bank (act as the banker in a game or in gambling)
- <u>S:</u> (v) bank (be in the banking business)
- <u>S:</u> (v) <u>deposit</u>, **bank** (put into a bank account) "She deposits her paycheck every month"
- <u>S</u>: (v) bank (cover with ashes so to control the rate of burning) "bank a fire"
- <u>S:</u> (v) <u>count, bet, depend, swear, rely</u>, **bank**, <u>look</u>, <u>calculate</u>, <u>reckon</u> (have faith or confidence in) "you can count on me to help you any time"; "Look to your friends for support"; "You can bet on that!"; "Depend on your family in times of crisis"

#### **Rules-Based Methods**

- Rules for sentiment analysis
  - If #(positive words) > #(negative words), then predict positive
  - How about this sentence:

Although CMPUT 651 might be interesting, it's less likely that I'll like it.

• There is an exception to every (NLP) rule!



## **Machine Learning**

- Supervised learning
  - Regression, classification
- Unsupervised learning
  - Clustering, PCA, etc.
  - Representation learning



#### **Supervised Learning**







### **Supervised Learning**



- **Training:** <X, Y> known for many samples
- Validation: <X, Y> also known
  - Pretend Y unknown and see model performance
  - Hyperparameter tuning, model selection
- **Test:** Given new X\*, predict Y\*
  - Industrial application: Deploy your system
  - Research: Y\* in fact also known, report test performance

### **Supervised Learning**

• E.g., sentiment analysis



- BoW (Indicator, tf·idf)
- N-gram features
- Sentiment lexicon
- NLP challenges:
  - Varying length
  - Unseen words



### **Supervised Learning**

• E.g., sentiment analysis



- Regression?
- Classification?
  - Binary
  - Multi-class



### **Supervised Learning**

• E.g., sentiment analysis



- Non-probabilistic
  - SVM, Fisher's discriminant
- Generative
  - Naive Bayes
- Discriminative
  - Logistic regression, softmax



### **Probabilistic Classification**



- Probabilistic modeling of X, Y
  - We can say something about p(X), p(Y), p(X, Y), p(X | Y), or p(Y | X)
  - Max a posterior inference <=> Minimal empirical loss

$$y = \operatorname{argmax} p(Y|\boldsymbol{x})$$





## **Probabilistic Classification**



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 $y = \operatorname{argmax} p(Y|\mathbf{x})$ 

- Generative model: Model p(X, Y)

$$p(Y|x) \propto_Y p(x, Y) = p(Y)p(x|Y)$$



## **Probabilistic Classification**



- Probabilistic modeling of X, Y
  - We can say something about p(X), p(Y), p(X, Y), p(X | Y), or p(Y | X)
  - Max a posterior inference <=> Minimal empirical loss  $y = \operatorname{argmax} p(Y|\mathbf{x})$
  - Discriminative model: Directly modeling p(Y|X)

# Naïve Bayes

- Inference objective  $y = \operatorname{argmax} p(Y|\mathbf{x})$
- Training objective: Maximize
  - $p(\mathcal{D}) = p(\{X^{(j)}, Y^{(j)}\}_{j=1}^m)$

$$= \prod_{j=1}^{m} p(Y^{(j)}) p(X^{(j)} | Y^{(j)})$$

$$= \prod_{j=1}^{m} p(Y^{(j)}) p(X^{(j)} | Y^{(j)})$$

$$= \prod_{j=1}^{m} \left[ p(Y^{(j)}) \prod_{i=1}^{m} p(X_i^{(j)} | Y^{(j)}) \right]$$
$$= \left[ \prod_{j=1}^{m} p(Y^{(j)}) \right] \left[ \prod_{y \in Y^{(j)} = y} p(X_i^{(j)} | y) \right]$$



max. joint prob.

data iid

Naive Bayes assumpt.

massaging

- Each factor is directly parametrized
- Maximum likelihood estimation for multinomial distributions is simply counting!



**CMPUT 651 (Fall 2019)** 

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# CMPUT 651 (Fall 2019) Logistic Regression

[classification task]

- Inference objective  $y = \operatorname{argmax} p(Y|\mathbf{x})$
- Training objective: Maximize

$$\begin{array}{ll} \mbox{maximize} & \prod_{j=1}^{n} p(Y^{(j)} | X^{(j)}) \\ \Leftrightarrow & \mbox{maximize} & \log \prod_{j=1}^{n} p(Y^{(j)} | X^{(j)}) \\ (\mbox{if optimum} & & p(Y^{(j)} | X^{(j)}) \\ & = \sum_{j=1}^{n} \log p(Y^{(j)} | X^{(j)}) \\ \Leftrightarrow & \mbox{minimize} & \sum_{j=1}^{n} \left[ -t^{(j)} \log y^{(i)} - (1 - t^{(j)}) \log(1 - y^{(j)}) \right] \end{array}$$

Abusing some notations

 $t^{(j)}$ : The ground truth label of  $Y^{(j)}$ ,  $t^{(j)} = 0$  or  $t^{(j)} = 1$  for binary classification

 $y^{(j)}$ : The predicted probability that  $Y^{(j)} = 1$ , i.e.,  $y^{(j)} \stackrel{\text{def}}{=} \Pr\{Y^{(j)} = 1 \mid x^{(j)}; \mathcal{M}\}$ 





# CMPUT 651 (Fall 2019) Logistic Regression

[classification task]

- Inference objective  $y = \operatorname{argmax} p(Y|\mathbf{x})$
- Training objective: Maximize

maximize

maximize



Statisticians seem to be pessimistic creatures who think in terms of losses. Decision theorists in economics and business talk instead in terms of gains (utility).

James O. Berger (1985). Statistical Decision Theory and Bayesian Analysis.

$$\Leftrightarrow \text{ minimize } \sum_{j=1}^{n} \left[ -t^{(j)} \log y^{(i)} - (1 - t^{(j)}) \log(1 - y^{(j)}) \right]$$

 $= \sum \log p(Y^{(j)} | X^{(j)})$ 

*j*=1

 $\prod p(Y^{(j)} | X^{(j)})$ 

 $\log \prod p(Y^{(j)} | X^{(j)})$ 

Abusing some notations

 $\Leftrightarrow$ 

(if optimum

is achieved)

 $t^{(j)}$ : The ground truth label of  $Y^{(j)}$ ,  $t^{(j)} = 0$  or  $t^{(j)} = 1$  for binary classification

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## Logistic Regression

- How can we model p(Y|X)?
  - Simplest case: linear classification
  - Obtain a score by  $s = \theta^{T} x + \theta_0$
  - Squash it as a probability  $y = p(Y = 1 | \mathbf{x}) = \text{sigmoid}(s) \stackrel{\text{def}}{=} \frac{1}{1 + e^{-s}}$

Graph for 1/(1+e^-x)





## Logistic Regression



- Why sigmoid?
  - Generalized linear model
    - x enters the model by linear transformation
    - y responses by exponential family
    - Why exponential family?
      - Most distributions we use are EXP
- Is it possible to use other functions to squash the distribution?
  - Yes. E.g., Probit regression (cdf of normal)



#### Logistic vs. Probit Regression







## Logistic Regression

• Training data  $\mathscr{D} = \{(\boldsymbol{x}^{(j)}, \boldsymbol{y}^{(j)})\}_{j=1}^n$ 

• Model 
$$y^{(j)} = \frac{1}{1 + e^{-(\theta_0 + \theta^T x^{(j)})}}$$

Model parameters:  $\Theta = (\theta_0, \theta)$ 

• Loss  

$$J = \sum_{j=1}^{n} \left[ -t^{(j)} \log y^{(i)} - (1 - t^{(j)}) \log(1 - y^{(j)}) \right]$$

• Optimization: gradient descent

$$\theta_i = \theta_i - \alpha \frac{\partial J}{\partial \theta_i}$$



### **Gradient Descent**

- Start from a (possibly) arbitrary position
- Take a mini-step against the gradient



### Gradient of LR

• For simplicity, we consider one sample

$$J = -t \log y - (1 - t) \log(1 - y)$$

• Steepest gradient descent

$$\frac{\partial J}{\partial \theta_i} = (y - t)x_i$$



### Mini-Batch

• Each data point i, we have defined loss  $J^{(i)}$ 

• We would like to optimize total loss 
$$J = \sum_{i=1}^{n} J^{(i)}$$

- We approximate J by a set of samples

$$J_{batch} = \sum_{i \in batch} J^{(i)}$$



#### Softmax

Multi-class classification

- Suppose target label  $t \in \{0, 1, \dots, n\}$
- For each target *i*, we compute the **logit**  $o_i = w_i^T x$
- Normalize logits are probabilities

$$p(Y = i) \stackrel{\Delta}{=} y_i \propto_i \exp\{w_i^{\top} x\} \qquad \text{positive}$$
$$y_i = \frac{\exp\{w_i^{\top} x\}}{\sum_i^{'} \exp\{w_{i'}^{\top} x\}} \qquad \text{normalizing}$$

Cross-entropy loss

$$J = -t_i \log y_i$$
 t: one-hot  
=  $-\log y[t]$  t: ID representation



Applying the single classifier to nearly all NLP tasks

• Part-of-speech (POS) tagging

This lecture is really boring article noun verb adverb adjective [Predict the tag among all candidate tags for a word]

Chunking

This lecture is really boring — | | — [Predict - or | for each two consecutive words]



#### Applying the single classifier to nearly all NLP tasks



[For each word, predict which word it depends on with what type]



#### Applying the single classifier to all NLP tasks



[For each consecutive components, predict if you'd like to further combine them and possibly what type?]



## Drawbacks of LR/Softmax

- Classification is non-linear
  - May not even represented as fixed-dimensional features
- Do not consider the relationship of labels within one data sample

lecture is really The boring determiner ? verb adverb adjective Three professors lecture IntroNLP

CardinalNumber ? Noun ProperNoune

https://www.merriam-webster.com/dictionary/lecture

#### lecture verb

**lectured**; **lecturing** \ 'lek-chə-riŋ , 'lek-shriŋ \

**Definition of** *lecture* (Entry 2 of 2) : a discourse given before an audience or (

intransitive verb



lecture noun

lec·ture | \'lek-chər , -shər\

**Definition of** *lecture* (Entry 1 of 2)

**2** : a formal reproof

## **Ungraded Homework**

- Derive Naïve Bayes, logistic regression again without referring to other materials
- Derive softmax derivative yourself
- Derive the decision boundary of LR/softmax
  - Decision boundary of Class *i* and Class *j*:  $\{x \in \mathbb{R}^n : p(Y = i | x) = p(Y = j | x)\}$

Do not submit ungraded homework

- Reading
  - Ch 4. Bishop, Pattern Recognition and Machine Learning
  - Ch 12. Jurafsky and Martin, Speech and Language Processing



# **Thank you!** Q&A

